

Department Of Engineering and Physics
Bachelor of Science (Honours) in Agricultural Engineering
Food Engineering

3 HOURS (100 MARKS)

INSTRUCTIONS

JUN 2024

Answer any **FOUR** questions. Each question carries 25 marks.

Question 1

- Use a Pearson Square to calculate the amounts of orange juice (10% sugar content) and sugar syrup (60% sugar content) needed to produce 50 kg of fruit squash containing 15% sugar. [5 marks]
- Peas which have an average diameter of 6 mm and a density of 880 kg m^{-3} are dried in a fluidised-bed drier. The minimum voidage is 0.4 and the cross-sectional area of the bed is 0.25 m^2 . Calculate the minimum air velocity needed to fluidise the bed if the air density is 0.96 kg m^{-3} and the air viscosity is $2.15 \times 10^{-5} \text{ N s m}^{-2}$. [5 marks]
- Calculate the component mass balance for mixing ingredients to make 25 kg of beef sausages having a fat content of 30%, using fresh beef meat and beef fat. Typically, beef meat contains 18% protein, 12% fat and 68% water and beef fat contains 78% fat, 12% water and 5% protein. [5 marks]
- Briefly explain five factors that affect the duration of completely frying foods. [10 marks]

Question 2

- Highlight five main advantages of fermentation as a method of food processing. [5 marks]
- Briefly explain four factors that affect the rate of food separation through a screen. [8 marks]
- Brewers' yeast is grown continuously in a fermenter with an operating volume of 12 m^3 . The residence time is 20 h and the yeast has a doubling time of 3.2 h. If a 2% inoculum, which contains 5% yeast cells is mixed with the substrate, calculate the mass of yeast harvested from the fermenter per hour. It is given that the density of broth is 1010 kg m^{-3} . [12 marks]

Question 3

- Milk containing 3.7% fat and 12.8% total solids is to be evaporated to a produce a product containing 7.9% fat. Assuming that there are no losses during the process, calculate:
 - the yield of product from 100 kg of milk and [5 marks]
 - the total solids concentration in the final product. [5 marks]
- Briefly describe five methods of peeling fruits and vegetables. [15 marks]

Question 4

- a. Corn meal with a moisture content of 18% (wb) is being extruded through a metering zone of an extruder with the following dimensions of the channel: width 8 cm, height 3 cm, length 65 cm. The wall velocity is estimated to be 0.35 m/s. The rheological properties of the extrudate can be estimated by a viscosity of 66,700 Pa s and a density of 1980 kg/m³. If the pressure drop is maintained at 3500 kPa, calculate the mass flow rate of extrudate through the die. [5 marks]
- b. Explain four factors that affect the degree of mixing solid food particles. [8 marks]
- c. Calculate the size of the motor required to blend olive oil and rape-seed oil in a ratio of 1 to 5 by a propeller agitator 20 cm in diameter operating at 750 rpm in a cylindrical tank of 1 m diameter at 20°C. It is given that P_o is 0.5, the viscosity of olive oil at 20°C is 0.084 Nsm⁻², the density of olive oil 910 kg m⁻³, the viscosity of rape-seed oil 0.118 Nsm⁻² and the density of rapeseed oil 900 kg m⁻³. [12 marks]

Question 5

- a. Highlight two advantages of ohmic heating as compared to microwave heating. [2 marks]
- b. An 8 kW oven has a hearth area of 4 m² and operates at 210°C. It is loaded with two batches of bread dough in baking tins; 150 loaves on the first batch and 120 loaves on the second batch. The surface of each loaf measures 12 cm x 20 cm. Assuming that the emissivity of dough is 0.85, that the dough bakes at 100°C, and that 90% of the heat is transmitted in the form of radiant energy, calculate the efficiency of energy use for each batch. [10 marks]
- c. Beer with a specific gravity of 1.042 and a viscosity of 1.40 x 10⁻³ N s m⁻² contains 1.5% solids which have a density of 1160 kg m⁻³. It is clarified at the rate of 240 l h⁻¹ in a bowl centrifuge which has an operating volume of 0.09 m³ and a speed of 10 000rpm. The bowl has a diameter of 5.5 cm and is fitted with a 4 cm outlet. If the bowl speed is increased to 15 000 rpm, calculate:
- i. the new feed rate, and [7 marks]
- ii. minimum rev particle size that can be removed at the new speed. [6 marks]

Question 6

- a. Explain four factors that influence the rate of heat transfer when freezing foodstuffs. [8 marks]
- b. Pulp which contains 15% solids is filtered in a plate and frame filter press with a pressure difference of 290 Pa and a 5.5 m² filter area. The masses of filtrate are shown below for a 1.5 h cycle.

Time (min)	7.5	30.4	50	90
Mass of filtrate (kg)	1800	3800	4900	6800

If the cake is incompressible and the viscosity of the filtrate is 1.33 x 10⁻³ Nsm⁻², calculate:

- i. the specific resistance of the cake, and [10 marks]
- ii. the volume of filtrate that would be obtained if the cycle time were reduced to 45 min. [7 marks]

End of paper

FOOD ENGINEERING (AEH308)

MATHEMATICAL FORMULAE

GRINDING AND CUTTING

$$dE/dL = KL^n$$

Kick

$$K = K_R f_c$$

$$dE/dL = K_R f_c L^{-1}$$

$$E = K_R f_c \log_e(L_1/L_2) \quad [\text{law}]$$

Rittinger

$$K = K_R f_c$$

$$dE/dL = K_R f_c L^{-2}$$

$$E = K_R f_c (1/L_2 - 1/L_1) \quad [\text{law}]$$

Bond

$$E = E_i (100/L_2)^{1/2} [1 - (1/q)^{1/2}] \quad [\text{law}]$$

$$q = L_1/L_2$$

Modification of the grinding energy equations

Energy required E (kWh/kg) for reducing particle size from x_1 to x_2

$$\text{Rittinger} \quad E = K_R \left(\frac{1}{x_2} - \frac{1}{x_1} \right)$$

$$\text{Kick} \quad E = K_k \ln \left(\frac{x_1}{x_2} \right)$$

$$\text{Bond} \quad E = K_B \left[\left(\frac{1}{x_2} \right)^{1/2} - \left(\frac{1}{x_1} \right)^{1/2} \right]$$

EXTRACTION / LEACHING / WASHING

$$\alpha = \frac{C_e}{C_r}$$

$$\Phi_v f C_f + \Phi_v s C_s = \Phi_v e C_e + \Phi_v r C_r$$

$$\frac{\text{Amount extracted}}{\text{Amount in raffinate}} = \frac{\phi_v e C_e}{\phi_v r C_r} = \alpha \frac{\phi_v e}{\phi_v r} = S$$

NB// for single stage

$$S = \frac{V_s}{V_r}$$

$$\text{Non extracted fraction} = 1 - f = \frac{C_r}{C_f} = \frac{1}{1 + S}$$

Where f=extracted fraction

$$f = \frac{\text{amount extracted}}{\text{amount in feed}} = \frac{\phi_v e C_e}{\phi_v f C_f}$$

$$\text{Therefore for only 1 stage, } f = \frac{S}{S+1}$$

For multistage:

$$N = \frac{\ln \left[\left(\frac{S-1}{1-f} \right) + 1 \right]}{\ln S} - 1$$

REFRIGERATION CHILLING AND FREEZING

Plank's equation

$$t_f = \left[\frac{(\rho \Delta H_L)}{(T_f - T_a)} \right] \left[\left(\frac{2Pr}{h} \right) + \left(\frac{4Rr^2}{\lambda} \right) \right]$$

ΔH_L = the latent heat of crystallisation of ice (334kJ/kg)

Shape factors

	Shape		
	Sphere	Infinite Plate	Infinite Cylinder
Shape factor	P=1/6, R=1/24	P=1/16, R=1/24	P=1/16, R=1/24

Pham's equation

$$t_f = \frac{1}{E} \left[\left(\frac{\Delta H_1}{\Delta T_1} \right) + \left(\frac{\Delta H_2}{\Delta T_2} \right) \right] \left[\left(\frac{r}{h} \right) + \left(\frac{r^2}{2\lambda} \right) \right]$$

$$\Delta T_1 = 0.5(T_i + T_{fm}) - T_a$$

$$\Delta T_2 = T_{fm} - T_a$$

$$\Delta H_1 = \rho C_{pu}(T_i - T_{fm})$$

$$\Delta H_2 = \rho \Delta H_L + \rho C_{pf}(T_{fm} - T_a)$$

$$T_{fm} = 1.8 + 0.263 T_{fm} + 0.105 T_a$$

$$\frac{\delta V}{\delta t} = \frac{A \Delta P}{\mu r \left[w \left(\frac{V}{A} \right) + L \right]}$$

$$\Delta P = \frac{V}{At} \times \mu r \left[w \left(\frac{V}{A} \right) + L \right]$$

$$E = 1 + \left[\frac{\left(1 + \left(\frac{2}{\beta_1} \right) \right)}{\left(\beta_1^2 + \left(\frac{2\beta_1}{\beta_1} \right) \right)} + \frac{\left(1 + \left(\frac{2}{\beta_1} \right) \right)}{\beta_2^2 + \left(\frac{2\beta_2}{\beta_1} \right)} \right]$$

The shape $\beta_1 = A/(\pi r^2)$

$$B_2 = 3V/(4\pi\beta_1 r^3)$$

$B_i = (hr)/\lambda$, Biot number

SEDIMENTATION

$$u = \frac{d_{st}^2 (\rho_s - \rho) g}{18\mu}$$

FILTRATION

$$\frac{\delta V}{\delta t} = \frac{A \Delta P}{R}$$

$$R = \mu r (L_c + L)$$

$$L_c = \frac{wV}{A}$$

$$R = \mu r \left[w \left(\frac{V}{A} \right) + L \right]$$



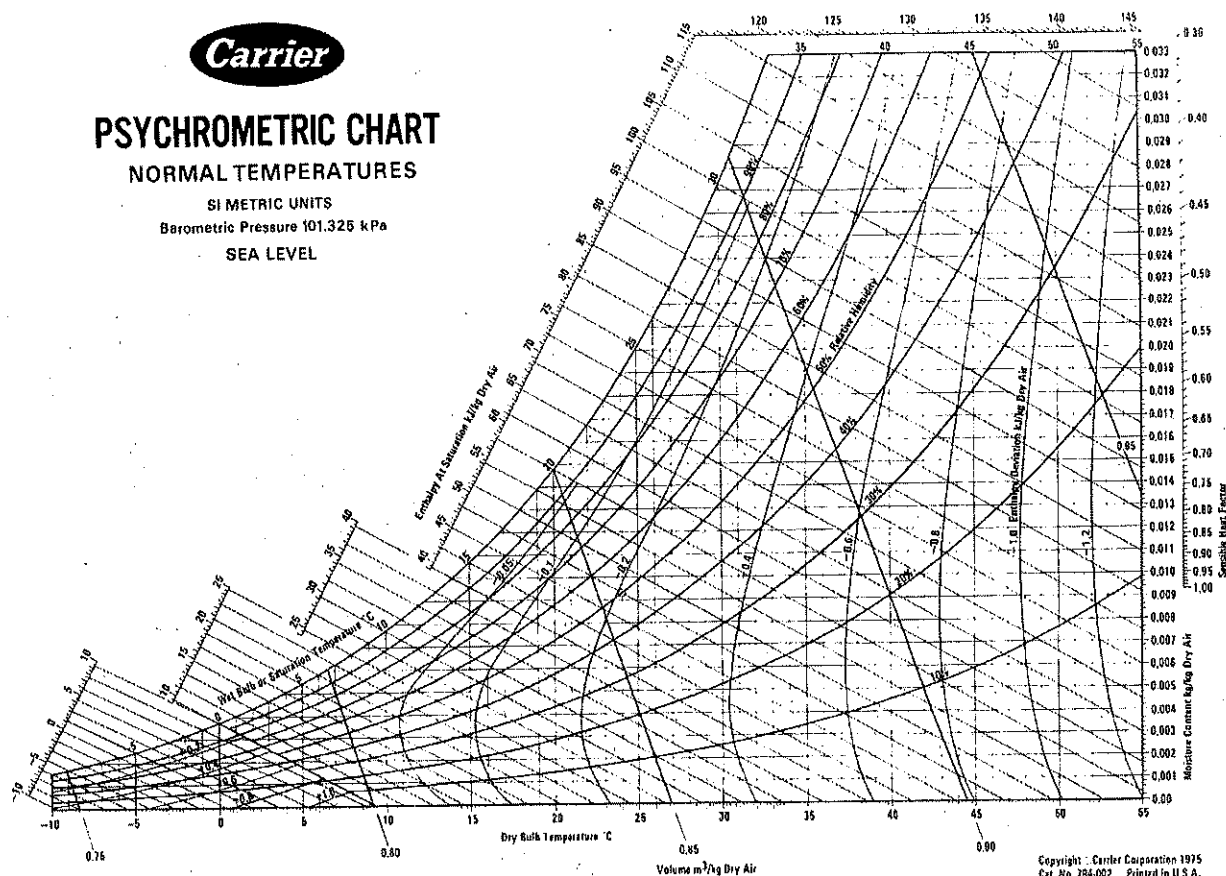
PSYCHROMETRIC CHART

NORMAL TEMPERATURES

SI METRIC UNITS

Barometric Pressure 101.325 kPa

SEA LEVEL



Below 0°C Properties and Enthalpy Deviation Lines Are For Ice

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