

**BINDURA UNIVERSITY OF SCIENCE EDUCATION**  
**FACULTY OF AGRICULTURE AND ENVIRONMENTAL SCIENCE**

AGM 213

**Department of Agricultural Economics, Education and Extension**  
**BSc Agricultural Science (Honours) Part II Examination**  
**ECONOMETRICS 1**

**3 HOURS (100 Marks)**

 **MAR 2023**

**INSTRUCTIONS**

Answer any **FOUR** questions. Each question carries **25 marks**.

**Marking guide: exam 2**

1. Consider a regression model of relating Y (the dependent variable) to X (the independent variable)  $Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$  where  $\varepsilon_i$  is the stochastic or error term. Suppose that the estimated regression equation is stated as  $\hat{Y}_i = \beta_0 + \beta_1 X_i$  and  $e_i$  is the residual error term.
  - a) Define  $e_i$  . **[2 marks]**
  - b) Explain how  $e_i$  is related to  $\varepsilon_i$ . **[5 marks]**
  - c) Explain four reasons for the inclusion of  $e_i$  in the population regression model. **[18 marks]**
2. In a study of fertility patterns a random sample of ten cows (X) was selected. Ten years later calves from each cow (Y) were counted. The following table contains the data for X and Y.

**Table 1:** Actual and Desired Number of calves of ten randomly selected cows

Cows	Actual(Y)	Desired(X)
1	0	0
2	2	1
3	1	2
4	3	1
5	1	0
6	3	3
7	4	4
8	2	2
9	1	2
10	2	1
SUM	19	16

a) Using data from Table 1:

Calculate the i) covariance

[5marks]

ii)  $\beta_0$

[5marks]

iii)  $\beta_1$

[5marks]

iv) Interpret the economic meaning of the estimated coefficients for  $\beta_0$  and  $\beta_1$ .

[10 marks]

3. Explain seven underlying assumptions for the classical linear regression model stated below:

$$Y_i = \beta_0 + \beta_1 X_i + \beta_2 Z_i + \epsilon_i$$

[25 marks]

4. Consider the following model

$$Y_t = \beta_0 + \beta_1 X_{1t} + \beta_2 X_{2t} + \epsilon_t$$

Where  $Y_t$  = actual rate of inflation (%) at time t,  $X_{2t}$  = unemployment rate (%) at time t, and  $X_{3t}$  = expected inflation rate (%) at time t. This model is known as the *expectations-augmented Phillips curve*.

As a test of this model, we obtained the data and the OLS method gave the following results.

$$Y_t = 7.1933 - 1.3925 X_{2t} + 1.4700 X_{3t}$$

$$R^2 = 0.50$$

a) Carefully state the meaning of the coefficients  $-1.3925$  and  $1.4700$  in the equation in terms of the impact of  $X_{2t}$  and  $X_{3t}$  on  $Y$ .

[5\*2 marks]

b) i) Interpret  $\bar{R}^2 = 0.50$ . [5 marks]

ii) Explain why does one prefer to use  $\bar{R}^2$  rather than  $R^2$ . [5 marks]

c) Suppose that you were told that the true value of  $\beta_1$  is  $-1.20$ . Explain if this shows whether the estimate is biased or not. [5 marks]

5. a) Explain the consequences of heteroscedasticity. [16 marks]

b) Explain two methods that are used for the detection of heteroscedasticity [9 marks]

6. Consider the following model

$$Y_t = \beta_0 + \beta_1 X_{1t} + \beta_2 X_{2t} + \varepsilon_t$$

Explain,

i) how a dummy variable is included in the above equation [15 marks]

ii) how to interpret a coefficient on a dummy variable [10 marks]

**End of Paper**