## BINDURA UNIVERSITY OF SCIENCE EDUCATION

## DME001: INTRODUCTORY MATHEMATICS

Time: 3 hours



Candidates may attempt ALL questions in Section A and at most TWO questions in Section B. Each question should start on a fresh page.

## SECTION A (40 marks)

Candidates may attempt ALL questions being careful to number them A1 to A6.

A1. Simplify the following:

(a) 
$$(-6+\sqrt{3})+(5-4\sqrt{3})$$
 [2]

(b) 
$$(2\sqrt{2} + \sqrt{5})(\sqrt{2} - 2\sqrt{5})$$
 [3]

(c) 
$$\frac{3-\sqrt{2}}{\sqrt{2}-5}$$

**A2.** (a) Find the remainder when 
$$3x^3 - x^2 - 5x + 2$$
 is divided by  $3x + 2$ . [2]

(b) Given 
$$x^2 + 2x - 3$$
 is a factor of  $f(x)$ , where  $f(x) \equiv x^4 + 6x^3 + 2ax^2 + bx - 3a$ . Find the value of  $a$  and of  $b$ .

A3. (a) Evaluate the following indicial expression, giving the final answers as an exact simplified fraction:  $(25^{\frac{1}{2}} + 81^{\frac{1}{4}})^{\frac{2}{3}}$  [3]

(b) Solve the following logarithmic equation for x,  $\log_a(x^2-10) - \log_a x = 2\log_a 3$ . [4]

A4. (a) Find the set of values of x, that satisfy the following inequality.

$$\frac{x}{2x-1} \ge 1 \tag{4}$$

(b) Express 
$$\frac{-12x + 5x^2 - 1}{(x+3)(x-1)^2}$$
 into partial fractions. [5]

**A5.** Given that  $z_1 = 13 + 6i$  and  $z_2 = 8 - 2i$ , find:

		_
	(a) $z_1 - z_2$	
	(b) $z_1 z_2$	2]
	(c) $\frac{z_1}{z_2}$	2]
	$z_2$	
A6.	A curve is given by $y^3 + y^2 + y = x^2 - 2x$ . Show that at the origin, $\frac{dy}{dx} = -2$ and	d
	1)	5]
	$dx^2$ 0, and give massiming some $x$	•
	SECTION B (60 marks)	
Con	didates may attempt TWO questions being careful to number them B7 to B9.	
Cano	ndates may attempt 1 wo questions being earlier to number them 2. To 11	
	da	
B7.	(a) Find $\frac{dy}{dx}$ in each of the following:	
	COAC .	2]
		4]
•		4]
	(b) A curve is defined by the parametric equations:	
	$x = 120t - 4t^2$ and $y = 60t - 6t^2$ .	
	Find the value of $\frac{dy}{dx}$ at each of the points where the curve crosses the $x-axis$ .	9
	(c) Find the coordinate of the turning point whose equation is $y = 2x^2 + 8x - 9$ and	
	determine the nature.	1]
В8.	(a) Express the equation $5sin2x = 4cos2x$ in the form $tan2x = k$ where k is constant.	a [2]
	(b) Integrate the following expressions with respect to x:	
	(i) $3x^3 - 4x^{\frac{1}{2}} + 24x - 2$	2
	(ii) $\frac{x^3+4}{x^2}$	[3]
	(iii) $\frac{2}{2x+3}$ from 0 up to 3.	[3]
	(iv) $xe^{4x}$ from 0 up to 1.	[8]
	$\frac{1}{2}$	
	(c) A curve has an equation $y = (4-x^2)^{-\frac{1}{2}}$ for $-1 \le x \le 1$ . The region R is enclosed	ed
	by $y = (4-x^2)^{-\frac{1}{2}}$ , the x-axis and the line $x = -1$ and $x = 1$ . Find the example of the constant $R$	act [5]
	value of the area $R$ .	
	(d) The sum to infinity of a geometric series is three times the first term of the series is a.	es.

- (i) Show that the common ratio of the geometric series is  $\frac{3}{2}$  [2]
- (ii) The third term of the geometric series is 81.
  - (1) Find the sixth term of the series. [2]
  - (2) Find the value of a as a fraction. [3]
- **B9.** (a) Show that  $\sin(75^{\circ}) = \frac{1+\sqrt{3}}{2\sqrt{2}}$  [5]
  - (b) Show that  $tan(A+B) = \frac{tan(A) + tan(B)}{1 tan(A) tan(B)}$  [9]
  - (c) Use Taylor series to expand  $sin(x + \frac{\Pi}{3})$  in ascending powers of x as far as the power of the term in  $x^4$ . [10]
  - (d) Using the binomial expansion, or otherwise, express  $(1+2x)^4$  in the form  $1+ax+bx^2+32x^3+16x^4$  where a and b are integers. [6]

END OF QUESTION PAPER